

Cambridge International AS & A Level

CANDIDATE NAME			
CENTRE NUMBER		CANDIDATE NUMBER	
MATHEMATIC	cs		9709/12
Paper 1 Pure N	Mathematics 1	A L L L	May/June 2023
		AUV	1 hour 50 minutes
You must answ	er on the question paper.		
You will need:	List of formulae (MF19)		

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [].

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This document has 20 pages. Any blank pages are indicated.

F	Find the equation of the curve.	
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	ossible values of the constant a .

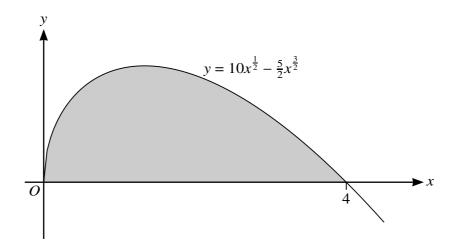


	in terms of the constant p .	
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(b)	Hence or otherwise find the set of values of p for which the equation $4x^2 - 24x$ real roots.	+ p = 0 ha
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Solve the equation $8x^6 + 215x^3 - 27 = 0$.	I
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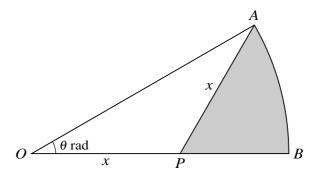
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The diagram shows the curve with equation $y = 10x^{\frac{1}{2}} - \frac{5}{2}x^{\frac{3}{2}}$ for x > 0. The curve meets the *x*-axis at the points (0, 0) and (4, 0).

Find the area of the shaded region.	[4]
	IEA A
	AFILA





The diagram shows a sector OAB of a circle with centre O. Angle $AOB = \theta$ radians and OP = AP = x. (a) Show that the arc length AB is $2x\theta \cos \theta$. [2] (b) Find the area of the shaded region APB in terms of x and θ . [4]

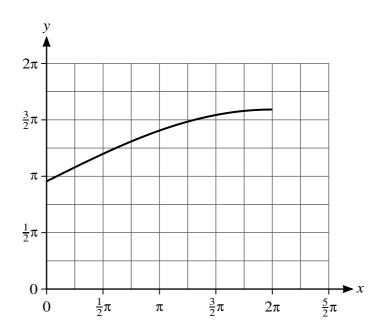


$(\cos\theta + \sin\theta)^2 = 1$	
for $0 \le \theta \le \pi$.	[3]
Hence verify that the only solutions of the equation $\cos \theta + \sin \theta$ 0 and $\frac{1}{2}\pi$.	$= 1 \text{ for } 0 \leqslant \theta \leqslant \pi \text{ are}$ [2]
2	
	for $0 \le \theta \le \pi$.

(b)	Duores the identity	$\sin \theta$	$1-\cos\theta$	$\cos \theta + \sin \theta - 1$	[2]
(D)	Prove the identity	$\frac{1}{\cos\theta + \sin\theta}$	$\frac{1}{\cos\theta - \sin\theta}$	$=\frac{1-2\sin^2\theta}{1}$.	[3]
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(c)	Using the results of	of (a)(ii) and (b), solve the equ	uation	
		$\sin \theta$	$1-\cos\theta$	2(2220 + 2220 - 1)	
		$\cos \theta + \sin \theta$	$\frac{\cos\theta - \sin\theta}{\cos\theta} = \frac{1}{2}$	$=2(\cos\theta+\sin\theta-1)$	
	for $0 \le \theta \le \pi$.				[3]
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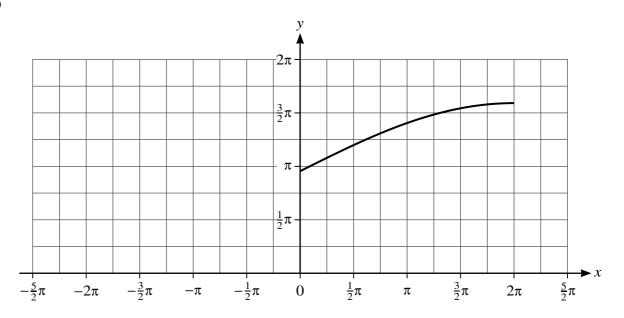
The diagram shows the graph of y = f(x) where the function f is defined by

$$f(x) = 3 + 2\sin\frac{1}{4}x \text{ for } 0 \le x \le 2\pi.$$

(a) On the diagram above, sketch the graph of $y = f^{-1}(x)$.	[2]
-----------------------------------------------------------------	-----

(b)	Find an expression for $f^{-1}(x)$.	[2]
		HEAD

(c)



The diagram above shows part of the graph of the function $g(x) = 3 + 2\sin\frac{1}{4}x$ for $-2\pi \le x \le 2\pi$.

	Complete the sketch of the graph of $g(x)$ on the diagram above and hence explain whether the function g has an inverse. [2]
(d)	Describe fully a sequence of three transformations which can be combined to transform the graph of $y = \sin x$ for $0 \le x \le \frac{1}{2}\pi$ to the graph of $y = f(x)$, making clear the order in which the transformations are applied. [6]



I	Find the two possible values of the first term.	
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(a)	Show that one possible value of a is 4 and find the other possible value.	
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11	The eq	uation	of a	curve	is

$$y = k\sqrt{4x+1} - x + 5,$$

where k is a positive constant.

(a)	Find $\frac{dy}{dx}$.	[2]
(b)	Find the x -coordinate of the stationary point in terms of k .	[2]
		AHEAD



Given that $k = 10.5$, find the equation of the normal to the curve at the pto the curve makes an angle of $tan^{-1}(2)$ with the positive x-axis.	
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Additional Page

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AHEAD



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