

# Cambridge International AS & A Level

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## MATHEMATICS

**9709/62**

Paper 6 Probability &amp; Statistics 2

May/June 2023

**1 hour 15 minutes**

You must answer on the question paper.

You will need: List of formulae (MF19)

## INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

## INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **16** pages. Any blank pages are indicated.

- 1 In a survey of 200 randomly chosen students from a certain college, 23% of the students said that they owned a car.

Calculate an approximate 93% confidence interval for the proportion of students from the college who own a car. [3]

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AHEAD

- 2 (a)** The random variable  $W$  has a Poisson distribution.

State the relationship between  $E(W)$  and  $\text{Var}(W)$ .

[1]

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- (b) The random variable  $X$  has the distribution  $B(n, p)$ . Jyothi wishes to use a Poisson distribution as an approximate distribution for  $X$ .

Use the formulae for  $E(X)$  and  $\text{Var}(X)$  to explain why it is necessary for  $p$  to be close to 0 for this to be a reasonable approximation. [1]

[1]

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- (c) Given that  $Y$  has the distribution  $B(20\,000, 0.000\,07)$ , use a Poisson distribution to calculate an estimate of  $P(Y > 2)$ . [3]

[3]

This image shows a blank sheet of white paper with horizontal ruling lines. The lines are evenly spaced and extend across the width of the page. In the bottom right corner, there is a small circular logo with a blue border and the word "AHEAD" written in white capital letters. The background of the entire image is black.

- 3 The masses, in kilograms, of newborn babies in country *A* are represented by the random variable  $X$ , with mean  $\mu$  and variance  $\sigma^2$ . The masses of a random sample of 500 newborn babies in this country were found and the results are summarised below.

$$n = 500 \quad \Sigma x = 1625 \quad \Sigma x^2 = 5663.5$$

- (a) Calculate unbiased estimates of  $\mu$  and  $\sigma^2$ . [3]

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AHEAD

A researcher wishes to test whether the mean mass of newborn babies in a neighbouring country,  $B$ , is different from that in country  $A$ . He chooses a random sample of 60 newborn babies in country  $B$  and finds that their sample mean mass is 2.95 kg.

Assume that your unbiased estimates in part (a) are the correct values for  $\mu$  and  $\sigma^2$ . Assume also that the variance of the masses of newborn babies in country  $B$  is the same as in country  $A$ .

(b) Carry out the test at the 1% significance level. [5]

[illegible]

- 4** The number,  $X$ , of books received at a charity shop has a constant mean of 5.1 per day.

- (a) State, in context, one condition for  $X$  to be modelled by a Poisson distribution. [1]

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Assume now that  $X$  can be modelled by a Poisson distribution.

- (b) Find the probability that exactly 10 books are received in a 3-day period. [2]

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- (c) Use a suitable approximating distribution to find the probability that more than 180 books are received in a 30-day period. [4]

[illegible]

The number of DVDs received at the same shop is modelled by an independent Poisson distribution with mean 2.5 per day.

- (d) Find the probability that the total number of books and DVDs that are received at the shop in 1 day is more than 3. [3]

[illegible]

- 5** (a) Two random variables  $X$  and  $Y$  have the independent distributions  $N(7, 3)$  and  $N(6, 2)$  respectively. A random value of each variable is taken.

Find the probability that the two values differ by more than 2. [5]

[illegible]



- Find the proportion of candidates who pass. [5]

[illegible]

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- HEAD



- 6** When a child completes an online exercise called a Mathlit, they might be awarded a medal. The publishers claim that the probability that a randomly chosen child who completes a Mathlit will be awarded a medal is  $\frac{1}{3}$ . Asha wishes to test this claim. She decides that if she is awarded no medals while completing 10 Mathlits, she will conclude that the true probability is less than  $\frac{1}{3}$ .

**(a)** Use a binomial distribution to find the probability of a Type I error. [2]

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The true probability of being awarded a medal is denoted by  $p$ .

**(b)** Given that the probability of a Type II error is 0.8926, find the value of  $p$ . [3]

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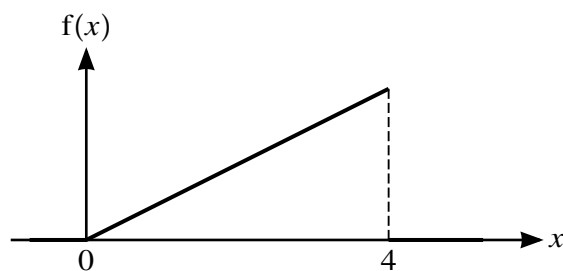
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7 (a)



The diagram shows the graph of the probability density function,  $f$ , of a random variable  $X$  which takes values between 0 and 4 only. Between these two values the graph is a straight line.

- (i) Show that  $f(x) = kx$  for  $0 \leq x \leq 4$ , where  $k$  is a constant to be determined. [2]

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- (ii) Hence, or otherwise, find  $E(X)$ . [3]

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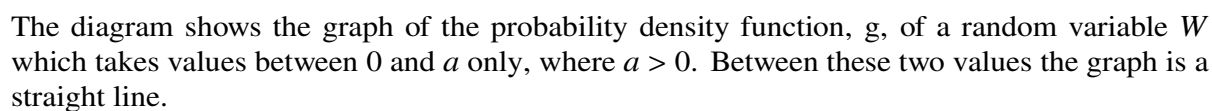
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Given that the median of  $W$  is 1, find the value of  $a$ . [3]

[illegible]

[illegible]



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