



- 1 Eggshells contain a high percentage by mass of calcium carbonate,  $\text{CaCO}_3$ . A student wants to find out what percentage of an eggshell is calcium carbonate and uses the following method.

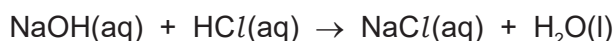
This method uses a known excess of acid to dissolve the eggshell. The amount of unreacted acid is then determined by titration with an alkali. Assume the acid only reacts with the  $\text{CaCO}_3$  in the eggshell.

- step 1** Wash an empty eggshell with distilled water.
- step 2** Warm the eggshell in an oven for a few minutes until dry.
- step 3** Grind the eggshell into a powder.
- step 4** Weigh approximately 2 g of the eggshell powder into a conical flask using a balance which measures to three decimal places.
- step 5** Add  $100\text{ cm}^3$  of  $2.00\text{ mol dm}^{-3}$  hydrochloric acid to the conical flask.
- step 6** Loosely cover the conical flask and leave for two days.
- step 7** Filter the contents of the conical flask, with any rinsings, into a  $250.0\text{ cm}^3$  volumetric flask and top-up to the mark using distilled water.
- step 8** Transfer  $25.00\text{ cm}^3$  of the solution prepared in **step 7** into a conical flask, add a few drops of thymol blue indicator and titrate against  $1.00\text{ mol dm}^{-3}$  sodium hydroxide using a  $50\text{ cm}^3$  burette.

The calcium carbonate in the eggshell reacts with the excess hydrochloric acid as follows.



The excess acid reacts with the sodium hydroxide solution as follows.



- (a) (i) Suggest how the student could confirm the eggshell is completely dry in **step 2**.

.....  
 ..... [1]

- (ii) State why the eggshell is made into a powder in **step 3** before making up the solution. Explain your answer.

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 ..... [1]

- (iii) Suggest why the solution is left for two days in **step 6** before being used.

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 .....

- (b) The student uses exactly 2.136 g of powdered eggshell and obtains the results shown in Table 1.1.

**Table 1.1**

| titration number                          | rough | 1     | 2     | 3     |
|---|-------|-------|-------|-------|
| final burette reading / cm <sup>3</sup>   | 16.55 | 32.85 | 16.10 | 32.30 |
| initial burette reading / cm <sup>3</sup> | 0.00  | 16.55 | 0.10  | 16.10 |
| titre / cm <sup>3</sup>                   |       |       |       |       |

- (i) Complete Table 1.1. Calculate the mean titre.

mean titre = ..... cm<sup>3</sup>  
[2]

- (ii) Calculate the amount, in mol, of unreacted HCl(aq) in the solution prepared in **step 7**. Show your working.

hydrochloric acid = ..... mol  
[2]

- (iii) Calculate the amount, in mol, of CaCO<sub>3</sub> that reacts with the excess of acid. Use your answer to calculate the percentage by mass of CaCO<sub>3</sub> in the eggshell. Show your working.

percentage by mass of CaCO<sub>3</sub> = ..... %  
[3]

- (c) Name a suitable piece of apparatus which could be used to transfer  $25.00\text{ cm}^3$  of solution in **step 8**.

..... [1]

- (d) In **step 4**, a conical flask is weighed using a balance accurate to three decimal places and the mass recorded. The eggshell is placed in the conical flask and the mass increases by  $2.136\text{ g}$ .

Calculate the percentage error in measuring the mass of this eggshell.

Show your working.

percentage error = ..... %  
[1]

- (e) State the effect on the percentage by mass if the eggshell is **not** completely dried in **step 2**.  
Explain your answer.

.....  
.....  
..... [1]

- (f) The student repeats the method using the same apparatus, but decides to use  $0.100\text{ mol dm}^{-3}$  NaOH(aq) to reduce the risk of corrosion or damage to eyes.

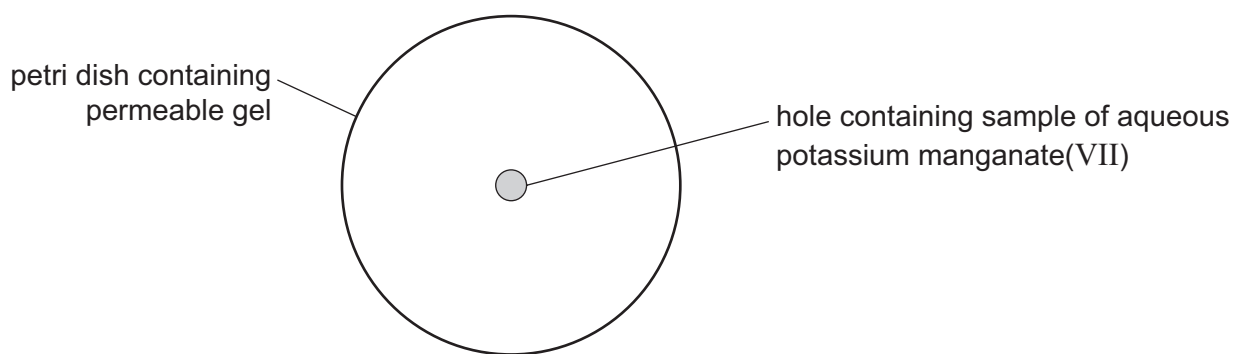
Explain how this introduces a weakness to the experimental procedure.

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..... [1]

[Total: 14]

**Question 2 starts on the next page.**

- 2 It is possible to measure the rate at which potassium manganate(VII),  $\text{KMnO}_4(\text{aq})$ ,  $M_r = 158$ , diffuses through a permeable gel using the following method.



**Fig. 2.1**

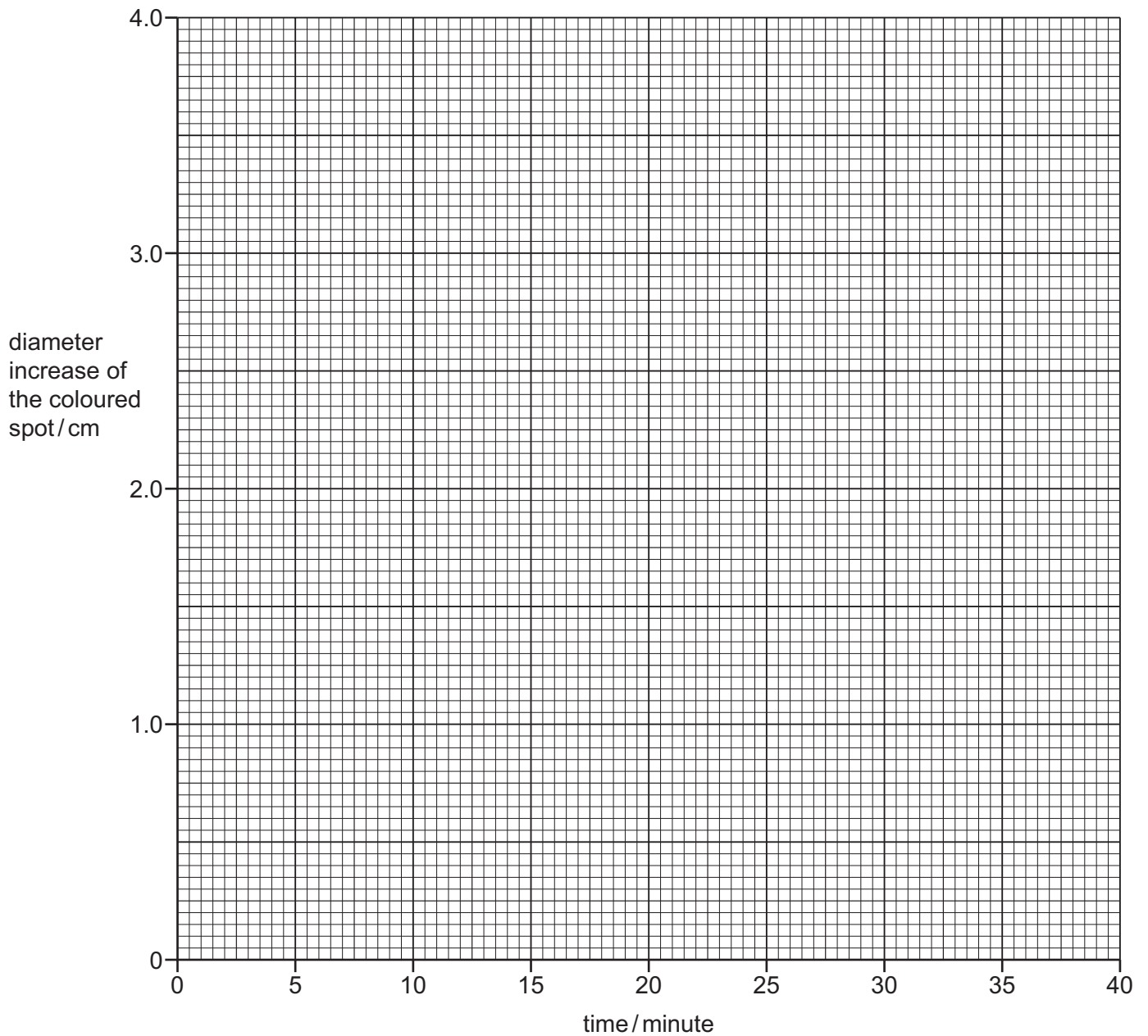
- step 1** A petri dish is prepared with a permeable gel.
- step 2** A hole of diameter 0.5 cm is cut in the centre of the permeable gel.
- step 3** A sample of  $\text{KMnO}_4(\text{aq})$  is placed into the hole and at the same time a stopwatch is started.
- step 4** After 3 minutes the diameter of the coloured spot is measured and recorded.
- step 5** The diameter is measured every 3 minutes until there are three successive equal measurements.

A student obtained the results shown in Table 2.1.

**Table 2.1**

| time / minute | diameter of the coloured spot / cm | diameter increase of the coloured spot / cm |
|---------------|------------------------------------|---|
| 0             | 0.5                                | 0.0   |
| 3             | 1.1                                | 0.6   |
| 6             | 1.7                                | 1.2   |
| 9             | 2.3                                | 1.8   |
| 12            | 2.7                                | 2.2   |
| 15            | 3.1                                | 2.6   |
| 18            | 3.2                                | 2.7   |
| 21            | 3.7                                | 3.2   |
| 24            | 3.9                                | 3.4   |
| 27            | 4.0                                | 3.5   |
| 30            | 4.1                                | 3.6   |
| 33            | 4.1                                | 3.6   |
| 36            | 4.1                                | 3.6   |

- (a) Plot a graph on the grid to show the relationship between diameter increase of the coloured spot and time. Use a cross (×) to plot each data point. Draw a line of best fit.



[2]

- (b) (i) On the graph, circle the point which you believe to be the most anomalous. [1]

- (ii) Suggest a possible explanation for this anomaly.

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..... [1]

- (c) Draw a suitable tangent to the line at time = 15 minutes. Calculate the gradient of your tangent. State both sets of coordinates used in your calculation. The stated coordinates must be from your tangent. Give the gradient to three significant figures.

coordinates 1 ..... coordinates 2 .....

gradient = .....  $\text{cm minute}^{-1}$  [3]

- (d) Select appropriate data from Table 2.1 and calculate the average rate of diffusion of  $\text{KMnO}_4(\text{aq})$  in  $\text{cm minute}^{-1}$ .

average rate of diffusion of  $\text{KMnO}_4 = \dots\dots\dots \text{cm minute}^{-1}$  [1]

- (e) Identify the independent variable in this experiment.

.....  
 ..... [1]

- (f) Suggest how the experiment could be made to be more reliable.

.....  
 ..... [1]

- (g) Another compound of potassium which is coloured is potassium dichromate(VI),  $\text{K}_2\text{Cr}_2\text{O}_7$ ,  $M_r = 294$ . This compound is corrosive when aqueous. It is possible to use the method described earlier to determine the rate of diffusion of  $\text{K}_2\text{Cr}_2\text{O}_7(\text{aq})$ .

- (i) Predict how the graph obtained for  $\text{K}_2\text{Cr}_2\text{O}_7(\text{aq})$  would differ from that obtained for  $\text{KMnO}_4(\text{aq})$ . Explain your answer.

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 .....  
 ..... [2]

- (ii) Apart from temperature, state **one** variable which must be controlled when comparing the rate of diffusion of  $\text{K}_2\text{Cr}_2\text{O}_7(\text{aq})$  and  $\text{KMnO}_4(\text{aq})$ .

.....  
 ..... [1]



- (h) (i) Other than wearing eye protection, state **one** safety precaution the student should take if they were to use potassium dichromate(VI).

.....  
..... [1]

- (ii) Another student suggests that to compare the rates of diffusion between  $K_2Cr_2O_7$  and  $KMnO_4$  it would be easier to place solid crystals of each of these compounds into the holes in two petri dishes of permeable gel.

Suggest **two** practical problems that this would cause.

1 .....  
.....  
2 .....  
..... [2]

[Total: 16]





**Important values, constants and standards**

|                                 |   |
|---------------------------------|---|
| molar gas constant              | $R = 8.31 \text{ J K}^{-1} \text{ mol}^{-1}$  |
| Faraday constant                | $F = 9.65 \times 10^4 \text{ C mol}^{-1}$   |
| Avogadro constant               | $L = 6.022 \times 10^{23} \text{ mol}^{-1}$   |
| electronic charge               | $e = -1.60 \times 10^{-19} \text{ C}$   |
| molar volume of gas             | $V_m = 22.4 \text{ dm}^3 \text{ mol}^{-1}$ at s.t.p. (101 kPa and 273 K)<br>$V_m = 24.0 \text{ dm}^3 \text{ mol}^{-1}$ at room conditions |
| ionic product of water          | $K_w = 1.00 \times 10^{-14} \text{ mol}^2 \text{ dm}^{-6}$ (at 298 K (25 °C))   |
| specific heat capacity of water | $c = 4.18 \text{ kJ kg}^{-1} \text{ K}^{-1}$ (4.18 J g <sup>-1</sup> K <sup>-1</sup> )  |

The Periodic Table of Elements

| Group |   |  |  |  |  |  |  |  |  |  |  |  |  |    |    |    |    |    |    |
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