

## Cambridge International AS & A Level

CANDIDATE NAME			
CENTRE NUMBER		CANDIDATE NUMBER	
MATHEMATI	cs		9709/12
Paper 1 Pure N	Mathematics 1	AH	tober/November 2021 1 hour 50 minutes
	ver on the question paper.		
You will need:	List of formulae (MF19)		

## INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

## **INFORMATION**

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [].

This document has 20 pages.

Solve the equation $2\cos\theta = 7 - \frac{3}{\cos\theta}$ for $-90^{\circ} < \theta < 90^{\circ}$ .	[4
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Describe fully the two single transformations that have been combined to give the resultransformation.	ılting [3]
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point $P(5,6)$ lies on the transformed curve $y = f(2x) = 3$	•••••
point $P(5, 6)$ lies on the transformed curve $y = f(2x) - 3$ . State the coordinates of the corresponding point on the original curve $y = f(x)$ .	
point $P(5, 6)$ lies on the transformed curve $y = f(2x) - 3$ .	[2]
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3	The function	fic	dofinad	as follows:

$$f(x) = \frac{x+3}{x-1}$$
 for  $x > 1$ .

(a)	Find the value of $ff(5)$ .	[2]
<b>(b)</b>	Find an expression for $f^{-1}(x)$ .	[3]
		HEAD



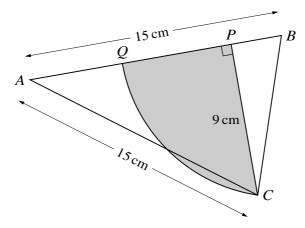
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	Find the exact value of $x$ . [3]
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)	Hence find the exact sum of the first 25 terms of the progression. [3
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In the diagram the lengths of AB and AC are both 15 cm. The point P is the foot of the perpendicular from C to AB. The length CP = 9 cm. An arc of a circle with centre B passes through C and meets AB at Q.

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8 (a)	It is given that in the expansion of $(4 + 2x)(2 - ax)^5$ , the coefficient of $x^2$ is $-1$	5.
	Find the possible values of $a$ .	[4]
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Find the values of $k$ and $a$ .	



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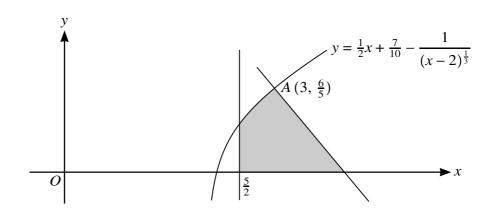
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10	The	function f is defined by $f(x) = x^2 + \frac{k}{x} + 2$ for $x > 0$ .
	(a)	Given that the curve with equation $y = f(x)$ has a stationary point when $x = 2$ , find $k$ . [3]

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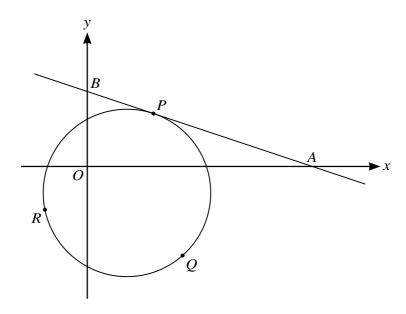


The diagram shows the line  $x = \frac{5}{2}$ , part of the curve  $y = \frac{1}{2}x + \frac{7}{10} - \frac{1}{(x-2)^{\frac{1}{3}}}$  and the normal to the curve at the point  $A\left(3, \frac{6}{5}\right)$ .

(a)	Find the $x$ -coordinate of the point where the normal to the curve meets the $x$ -axis. [5]	]
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The diagram shows the circle with equation  $x^2 + y^2 - 6x + 4y - 27 = 0$  and the tangent to the circle at the point P(5, 4).

(a) The tangent to the circle at P meets the x-axis at A and the y-axis at B.

Find the area of triangle $OAB$ , where $O$ is the origin.	[5]
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Find the exact area of triangle $PQR$ .	
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## **Additional Page**

If you use the following lined page to complete the answer(s) to any question(s), the question number(s) must be clearly shown.

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