Cambridge Assessment International Education

Cambridge International AS & A Level

MATHEMATICS **9709/42**

Paper 4 Mechanics **March 2020**

MARK SCHEME

Maximum Mark: 50

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the March 2020 series for most Cambridge IGCSE™, Cambridge International A and AS Level components and some Cambridge O Level components.

This document consists of **13** printed pages.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:
Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:
Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:
Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:
Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:
Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Mathematics-Specific Marking Principles	
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

Mark Scheme Notes

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

B Mark for a correct result or statement independent of method marks.

DM or **DB** When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly, when there are several B marks allocated. The notation DM or DB is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.

FT Implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only.

Abbreviations

AEF/OE	Any Equivalent Form (of answer is equally acceptable) / Or Equivalent
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
CAO	Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
CWO	Correct Working Only
ISW	Ignore Subsequent Working
SOI	Seen Or Implied
SC	Special Case (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)
WWW	Without Wrong Working
AWRT	Answer Which Rounds To

Question	Answer	Marks	Guidance
1(a)	Power = 750000/10 = 75000 W or 75 kW	**B1**	Power = WD/Time
		1	
1(b)	Driving force DF = 75000/25	**B1FT**	Using $P = \text{DF} \times v$
	[DF – 2400 = 16000a]	**M1**	Using Newton's 2nd law
	$a = 0.0375$ ms^{-2}	**A1**	Allow $a = \frac{3}{80}$
		3	

Question	Answer	Marks	Guidance
2(a)	$[1.44 = 0 + ½ \times 2t^2]$	**M1**	For using a complete method which would lead to an equation for finding a value of t such as $s = ut + ½\ at^2$ with $u = 0$, $s = 1.44$ and $a = 2$
	$t = 1.2$ s	**A1**	
		2	
2(b)	$R = 0.4g - 3 \times \frac{3}{5} = 0.4g - 3 \sin 36.9$ [= 2.2]	**B1**	
	$[3 \times \frac{4}{5} - F = 3 \cos 36.9 - F = 0.4 \times 2]$ $[F = 1.6]$	**M1**	Use Newton's 2nd law, 3 terms, to find F.
	$\left[\mu = \frac{3 \times \frac{4}{5} - 0.4 \times 2}{0.4g - 3 \times \frac{3}{5}} = \frac{1.6}{2.2}\right]$	**M1**	Use of $\mu = \frac{F}{R}$
	$\mu = 0.727$	**A1**	Allow $\mu = \frac{8}{11}$
		4	

Question	Answer	Marks	Guidance
3(a)	Initial KE = $\frac{1}{2} \times 0.2 \times 5^2$ or Final KE = $\frac{1}{2} \times 0.2 \times 3^2$	**B1**	
	$\frac{1}{2} \times 0.2 \times 5^2 = 0.2gh + \frac{1}{2} \times 0.2 \times 3^2$	**M1**	Use conservation of energy
	$h = 0.8$	**A1**	
		3	
3(b)	Apply work-energy equation from A to C	**M1**	
	$\frac{1}{2} \times 0.2 \times 5^2 - 3.1 + 0.2g \times 0.5 = \frac{1}{2} \times 0.2v^2$	**A1**	Correct work-energy equation
	Speed = 2 ms^{-1}	**A1**	
		3	

Question	Answer	Marks	Guidance
4(a)	Use the constant acceleration equations to obtain an expression for either s_{AB} or s_{BC} in terms of a	**M1**	
	$s_{AB} = 2 \times 4.5 - ½ \times a \times 2^2$	**A1**	**or** $s_{AB} = ½(v_A + v_B) \times 2 = 9 - 2a$
	$s_{BC} = 2 \times 4.5 + ½ \times a \times 2^2$	**A1**	**or** $s_{BC} = ½(v_B + v_C) \times 2 = 9 + 2a$
	$[2 \times 4.5 - ½a \times 2^2 = \frac{4}{5}\ (2 \times 4.5 + ½a \times 2^2)]$	**M1**	Use the given information to find a valid equation for a
	$a = 0.5\ \text{ms}^{-2}$	**A1**	
	Alternative method for question 4(a)		
	$[4.5 = u + 2a,\ s_{AC} = 4u + 8a,\ s_{AB} = 2u + 2a]$	**M1**	Any two relevant equations in u, a, s_{AB} and s_{AC} where u is the velocity at A
	Two correct equations	**A1**	
	Three correct equations	**A1**	
	$[2(4.5 - 2a) + 6a = \frac{5}{4}\ \{2(4.5 - 2a) + 2a\}]$	**M1**	Use the given information that $BC = {}^5/_4 AB$ to find a valid equation such as the one shown OE involving a only
	$a = 0.5\ \text{ms}^{-2}$	**A1**	
	Alternative method for question 4(a)		
	$[AC = 4.5 \times 4]$	**M1**	Using $AC = v_B \times 4$ since v_B is the average velocity over AC
	$BC = 5/9 \times AC$ **or** $AB = 4/9 \times AC$	**M1**	
	$BC = 10$ or $AB = 8$	**A1**	
	$[10 = 4.5 \times 2 + 2a$ **or** $8 = 4.5 \times 2 - 2a]$	**M1**	Using $s = ut + ½\ at^2$ for BC **or** $s = vt - ½\ at^2$ for AB
	$a = 0.5\ \text{ms}^{-2}$	**A1**	

Question	Answer	Marks	Guidance
		5	
4(b)	$s_{AB} = 2 \times 4.5 - ½ \times 0.5 \times 2^2 = 8$ **OR** $s_{BC} = 2 \times 4.5 + ½ \times 0.5 \times 2^2 = 10$	**M1**	Attempt to find the value of s_{AB} or s_{BC} **OR** attempt to find s_{AB} directly as $s_{AC} = 3.5 \times 4 + ½ \times a \times 4^2$ or ½ $(4.5 - 2a + 4.5 + 2a) \times 4$ **or** add the 2 expressions found in **4(a)** for s_{AB} and s_{BC}
	$s_{AC} = 8 + {}^5/_4 \times 8 = 18$ m **OR** $s_{AC} = 10 + {}^4/_5 \times 10 = 18$ m	**A1**	
		2	

Question	Answer	Mark	Guidance
5(a)	[4 sin 30 + F sin 60 – 6 = 0]	**M1**	Resolve forces vertically and equate to zero
	Correct equation	**A1**	
	$F = 4.62$	**A1**	Allow $F = \frac{8}{\sqrt{3}}$ or $F = \frac{8}{3}\sqrt{3}$
		3	

Question	Answer	Marks	Guidance
5(b)	Resolve forces either vertically or horizontally	**M1**	
	$F \sin \alpha + 4 \sin 30 - 6 = 0$ and $F \cos \alpha + 3 - 4 \cos 30 = 0$	**A1**	Both equations correct [$F \sin \alpha = 4$] [$F \cos \alpha = 0.464102...$]
	$[F^2 = 4^2 + 0.464^2]$ or $\left[F = \frac{4}{\sin 83.4} = \frac{0.464}{\cos 83.4}\right]$	**M1**	Attempt to solve for F using Pythagoras or from a value found for α
	$\left[\alpha = \tan^{-1}\left(\frac{4}{0.464}\right)\right]$ or $\left[\alpha = \sin^{-1}\left(\frac{4}{4.03}\right) = \cos^{-1}\left(\frac{0.464}{4.03}\right)\right]$	**M1**	Attempt to solve for α using trigonometry or from a value found for F
	$F = 4.03$ and $\alpha = 83.4$	**A1**	Both correct as shown [$F = 4.0268\ldots$, $\alpha = 83.382\ldots$]
		5	

Question	Answer	Marks	Guidance
6(a)	$[T - 200 = 700 \times -12]$ Car: $-T - 600 - F = 1600 \times -12$ System: $-600 - 200 - F = 2300 \times -12$	**M1**	Apply Newton's 2nd law to the trailer or apply Newton's 2nd law to the car and to the system and eliminate the braking force, F.
	Magnitude of $T = 8200$ N	**A1**	
		2	
6(b)	Car $[T - F - 600 = 1600 \times -12]$ or System $[-600 - 200 - F = 2300 \times -12]$	**M1**	Apply Newton's second law either to the car or to the system with braking force = F and use of *their* T from **6(a)**
	Braking force $F = 26800$ N	**A1**	
		2	
6(c)	$[v^2 = 22^2 + 2 \times -12 \times 17.5]$	**M1**	A complete method using constant acceleration equations which would lead to an equation for finding v, using $u = 22$, $s = 17.5$ and $a = -12$
	$v = 8$ ms^{-1}	**A1**	AG
		2	
6(d)	$[2300 \times 8 + m \times 0 = 2300 \times 2 + m \times 5]$	**M1**	For applying the conservation of momentum equation to the system of car, trailer and van, where m = mass of the van
		A1	Correct equation
	$m = 2760$ kg	**A1**	
		3	

Question	Answer	Marks	Guidance
7(a)	$[v = 2t - 3]$	**M1**	For differentiation of s for $0 \leqslant t \leqslant 6$
	$t = 1.5$	**A1**	
		2	
7(b)	Velocity at arrival = 9 ms^{-1}	**B1**	$t = 6$ used in v
	$v = -\frac{24}{t^2} - 0.5t$	**M1**	For differentiation of s for $t \geqslant 6$
	Velocity when leaves = –3.67 ms^{-1}	**A1**	Allow $v = -11/3$
		3	
7(c)	At $t = 0$, $s = 2$ **or** at $t = 6$, $s = 20$	**B1**	SOI
	At $t = 1.5$, $s = -0.25$	**B1**	SOI
	At $t = 10$, $s = 2.4$	**B1**	SOI
	[Total distance = 2 + 0.25 + 0.25 + 20 + (20 – 2.4)]	**M1**	Evidence of distance rather than displacement involving all three sections, (0, 1.5), (1.5, 6) and (6, 10)
	So total distance travelled = 40.1 m	**A1**	
		5	